

Fig. 2. (a) Guided-mode dispersion characteristics of structure-I along with a typical beam-mode dispersion line $\beta (= v/c) = 0.5$, the shaded and non-shaded regions indicating the non-radiating and radiating regimes and (b) Inside-slit and far-field (magnified 25 times) FFT spectrum of the E_x field of structure-I. (c) E_x field pattern at the typical angular frequency $\omega (= 2\pi c/p)$ of 0.12 for structure-I showing fields confined to the top and bottom surfaces.

3. Out-coupling of guided modes

The limitation of structure-I in coupling out Cerenkov radiation from the top and bottom surfaces of the structure in the transverse direction is overcome in the proposed structure-II. This is accomplished by modifying structure-I, introducing a change in the metamaterial slab thickness between h and $h + h'$ periodically at a regular interval of slits, typically four, which consequently introduces an additional periodicity ($p' = 4p$) in the axial direction of the structure geometry (structure-II) as shown in Fig. 1(b). This suggestion stems from the well known concept of the Brillouin-zone band folding phenomenon in the superlattice-based photonic crystal arising out of the reduction of the size of the first Brillouin zone of the guided-mode dispersion diagram caused by the introduction of the additional periodicity due to the larger size of the unit cell and the reduced symmetry of the crystal [13,14,17]. Let us now consider an electron bunch close to and above the top surface of structure-II moving with a velocity that is synchronous with the phase velocity of a mode supported by the structure and causing the excitation of modes in the unfolded regime of the dispersion diagram as shown in Fig. 3(a). However, it is likely that some of these modes excited in structure-II would be driven into a reduced Brillouin zone as compared to structure-I in view of the unit cell size along x of structure-II becoming p'/p times larger than that of structure-I, which is therefore likely to result in the folding of the guided modes at $k_x = \pi/p'$ [18]. Figure 3(a) shows the folded bands which are obtained by translating the guided bands of structure-I by an appropriate reciprocal lattice vector conforming to the Brillouin-zone folding effect [14,17,18]. In the present context, the wave number (momentum) of each of the modes, lying on the positive side of the band-folding symmetry ($k_x = \pi/p'$) on the momentum (k_x) scale [17,18], is translated into negative side of the band-folding symmetry, with the guided-mode frequency remaining unchanged as shown in Fig. 3(a). The amount of this translation is equal to the separation between the point of symmetry $k_x = \pi/p'$ and the momentum of the guided mode.

Typically, out of the first four guided modes of structure-II excited by the electron bunch at the angular frequencies $\omega (= 2\pi c/p)$ of 0.05, 0.085, 0.12 and 0.145, respectively, while the first of these excited modes at $\omega (= 2\pi c/p) = 0.05$ remains in the unfolded regime, the remaining three are in the folded regime with their respective momenta shifted through band folding from the unfolded regime. Further, out of the three modes in the folded regime, while one, at $\omega (= 2\pi c/p) = 0.085$, is in the guided regime ($k_x > \omega/c$), the remaining two modes, at $\omega (= 2\pi c/p) = 0.12$ and 0.145, are within the light zone ($k_x < \omega/c$), which would exhibit far-field peaks in the FFT spectrum at these two frequencies corresponding to the far-field radiation from structure-II. Figure 3(b) shows the FFT spectrum far field radiation from structure-II. The phenomenon of the coupling out of radiation can also be appreciated from

the E_x -field pattern of structure-II, typically illustrated at $\omega(=2\pi c/p)=0.12$ as shown in Fig. 3(c) vis-à-vis the corresponding field pattern of structure-I showing no such radiation as shown in Fig. 2(c).

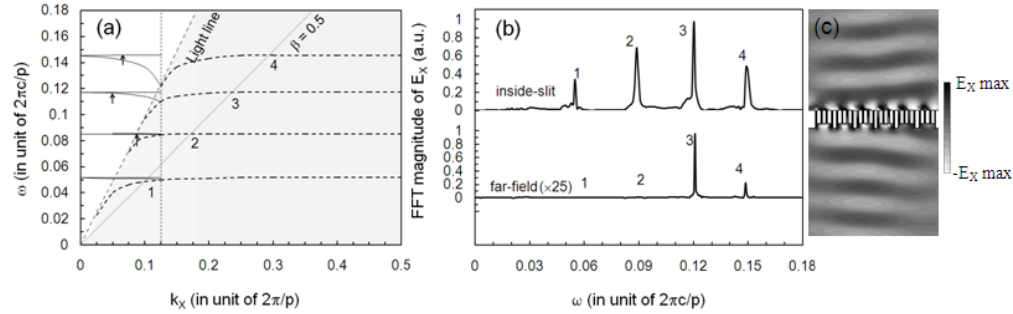


Fig. 3. (a) Guided-mode dispersion characteristics of structure-II, along with a typical beam-mode dispersion line $\beta(v/c) = 0.5$, the shaded and non-shaded regions indicating the non-radiating and radiating regimes, respectively. The first four lower dispersion intersecting points are represented by 1, 2, 3 and 4, respectively. The folded bands are shown in solid lines, with the vertical dotted line indicating band-folding symmetry and with the points indicated by the arrows on the folded dispersion curve representing the points at which the momentums corresponding to points 2, 3 and 4, respectively, are shifted due to band folding. (b) Inside-slit and far-field (magnified 25 times) FFT spectrum of the E_x field of structure-II. (c) E_x field pattern at the typical angular frequency ($\omega = 2\pi c/p$) of 0.12 for structure-II showing fields radiated from the top and bottom surfaces.

4. Comparison of radiation intensity with that of reflection grating

The radiation intensity, measured in terms of the square of the amplitude of the axial electric field, from structure-II is compared to that from a reflection grating [19] under identical conditions. Figure 4 shows the comparison of radiation intensity of structure-II with that of reflection grating. For this purpose, we consider both the structures in close proximity to a moving electron bunch of typical energy corresponding to the dimensionless axial velocity $\beta(v/c) = 0.5$. We also consider the identical axial periodicity (p') and identical width (w) for the reflection grating and optimize its groove depth to the value of $H' = 0.44p'$, as indicated in the inset of Fig. 4, at an angular frequency $\omega(=2\pi c/p) = 0.12$, for the maximum Smith-Purcell radiation intensity in a direction normal to the grating surface. At this frequency, structure-II also shows the far-field peak as shown in Fig. 3(b). It is clearly seen from Fig. 4 that the proposed structure-II is superior to the reflection grating in term of the intensity of the radiation. This enhanced radiation capability of structure-II in comparison with the reflection grating can be attributed to the phenomenon of coupling of Cerenkov radiation generated via Brillouin-zone band folding in structure-II, which is absent in the reflection grating where the surface electromagnetic waves supported by a grating are known to be excited by the moving electron bunch, and which, however, cannot contribute to the far-field radiation [20,21].

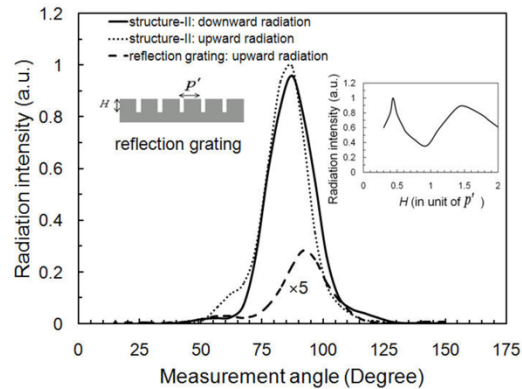


Fig. 4. Angular dependence of the far-field radiation of structure-II compared to that of the reflection grating (magnified 5 times) at an angular frequency $\omega (= 2\pi c/p)$ of 0.12, the measurement angle being the angle between the direction of the moving electron bunch and that of the radiation, with the inset showing the variation of the radiation intensity of the reflection grating with the grating groove depth having a moving electron bunch energy level corresponding to $\beta (= v/c) = 0.5$.

4. Conclusion

We have demonstrated that Cerenkov radiation generated inside metallic metamaterial slabs can be out-coupled via the mechanism of Brillouin-zone band folding and implemented by the proposed new structure, which is essentially a modified metamaterial slab (structure-I) in which additional periodicity is introduced (structure-II). The new structure interacting with a moving electron bunch proves to be better than the reflection grating structure with respect to the radiation intensity from the structure. The structure, being metallic, appears to enjoy an obvious edge over any dielectric Cerenkov device in terms of circumventing adverse effects such as the dielectric breakdown, the dielectric charging that incurs heating if the dielectric is lossy, and the issues arising from the cooling of the device. All-metal metamaterial structure studied in this paper can be a good candidate as an interaction structure for a terahertz source

Acknowledgments

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