# Tutorials in Complex Photonic Media

## Editors:

Mikhail A. Noginov Graeme Dewar Martín W. McCall Nikolay I. Zheludev



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## **Foreword**

Classical optics has been with us for some considerable time, yet the past decade has produced a cornucopia of new research, often revealing unsuspected phenomena hidden like nuggets of gold in the rich lode of optical materials. The key has often been complexity. The range of optical properties available in natural materials is limited, but by adding manmade structure to nature's offerings we can extend our reach, sometimes to achieve properties not seen before. I pick one example from the many included in this volume: negative refraction. Years ago it had been realised that a material with negative magnetic and electric responses would also have a negative refractive index. There, the idea languished for nearly half a century, lacking the naturally occurring materials to realise the effect. However by internally structuring a medium on a scale less than the relevant wavelength, it was proved possible to make a new form of material, a 'metamaterial,' which had the required negatively refracting properties. This concept alone has given rise to thousands of papers. There are other examples I could cite from the chapters in this book: exploitation of nearfield properties of nanoparticle arrays, photonic band gap waveguides, metallic nanostructures for sensing proteins, and so on. All of these examples have in common that man adds complexity to the offerings of nature.

In the face of these myriad advances, how are students or other new entrants to the field to educate themselves in the new technology? This book provides the answer, collecting together a definitive series of tutorials, each provided by an expert in the field. It is published at a time when there are many such new entrants and will be of great value.

J. B. Pendry Imperial College London

## **Preface**

An increasingly large number of high- and low-tech technologies and devices benefit from employing optics and photonics phenomena, the latter originally being termed photon-based electronics. Progress in the research fields of optics and photonics, which have both experienced continuously strong growth over the last few decades, critically depends on the understanding and utilization of the physical, chemical and structural properties of optical materials. The optical materials used in traditional optics technology were macroscopically homogeneous in that their scale of inhomogeneity was much less than the wavelength. In more recent years, multiple breakthroughs have involved inhomogeneous, composite, and multiphase materials, whose structures are either photoinduced or determined by synthesis or fabrication. Examples include holography, optics of scattering media, and metamaterials. These breakthroughs make photonic materials inherently complex. The broad range of physical phenomena underlying complex photonic media makes it difficult for scientists, engineers, and students entering the field to navigate through the range of topics and to understand clearly how they relate to each other.

The purpose of this book is to provide the necessary coverage and inspire the reader's curiosity about the fascinating subject of complex photonic media. All of the tutorial chapters are designed to start with the basics and gradually move toward discussion of more advanced topics. We thus envisage that students and scholars with diverse backgrounds and levels of expertise will find this text interesting and useful. The book can be used as a supplemental text in courses on nanotechnology or optical materials, or a variety of other courses. It can also be used as the main text in a more focused course aimed at fundamental properties of scattering media and metamaterials. The anticipated level of preparation is equivalent to advanced senior undergraduate level, beginning graduate level, or higher. The book covers the topics in the following (rather loose) categorization:

Negative index materials (NIMs). One of the most exciting developments in complex photonic media in recent years is the realization that the basic parameters describing the electromagnetics of simple, isotropic media can take simultaneously negative values. This leads to all kinds of interesting phenomena, from a revised understanding of Snell's law, to lenses that defeat the conventional diffraction resolution limit. In "Negative Refraction" (Chapter 1), Martin W. McCall and Graeme Dewar describe the basic theory and impetus for negative refraction research. In "Optical Hyperspace: Negative Refractive Index

and Subwavelength Imaging" (Chapter 2), Leonid V. Alekseyev, Zubin Jacob, and Evgenii Narimanov explore nonmagnetic routes that exploit materials with hyperbolic dispersion relations.

Magneto-optics. The term magneto-optics is used when the direction and polarization state of light are controlled by the application of external magnetic fields, offering opportunities for optical storage and isolation in optical systems. In "Magneto-optics and the Kerr Effect with Ferromagnetic Materials" (Chapter 3), Allan D. Boardman and Neil King introduce the magneto-optics derived from air-ferroelectric interfaces and glass/ferromagnetic film/air multilayer systems. "Nonlinear Magneto-Optics" (Chapter 4) by Yutaka Kawabe gives emphasis to the relationship between the tensors describing the nonlinearity and the underlying crystal point group symmetry. In "Optical Magnetism in Plasmonic Metamaterials" (Chapter 5), Gennady Shvets and Yaroslav A. Urzhumov describe some of the difficult challenges that lie ahead for achieving magnetic activity at optical frequencies.

Chiral media and vortices. Light, being composed of unit spin photons, is inherently chiral. However, chirality in optical systems can also be engaged at structural and macroscopic electromagnetic levels. Structural chirality is covered by Ian Hodgkinson and Levi Bourke in "Chiral Photonic Media" (Chapter 6), which describes the multilayer matrix formalism for novel elliptically polarized filters. When optical beams interfere, phase singularities occur; in "Optical Vortices" (Chapter 7) Kevin O'Holleran, Mark R. Dennis, and Miles J. Padgett describe some of the remarkable topological knots and 3D twists that result.

Scattering in periodic and random media. Scattering of light is fundamental to complex photonic media. Structures that are periodic are generally referred to as photonic crystals. In "Photonic Crystals: From Fundamentals to Functional Photonic Materials" (Chapter 8), Durga P. Aryal, Kosmas L. Tsakmakidis, and Ortwin Hess describe how photonic bandstructure emerges in both 1- and 2D structures, and how optical switching is achievable in inverse-opal structures. When the material inhomogeneity is random, different methods must be employed. In "Wave Interference and Modes in Random Media" (Chapter 9), Azriel Z. Genack and Sheng Zhang describe photon transport in a medium in terms of the interference of multiply scattered partial waves as well as by considering the different spatial, spectral, and temporal characters of the electromagnetic modes.

Photonic media with gain and lasing phenomena. Photonic media with gain and lasing phenomena represents the generic class of active photonic media. "Chaotic Behavior of Random Lasers" (Chapter 10) by Diederik Wiersma, Sushil Mujumdar, Stefano Cavalieri, Renato Torre, Gian-Luca Oppo, and Stefano Lepri examines the irreproducibility of experimental emission spectra and the change of statistics at near threshold. "Lasing in Random Media" (Chapter 11) by Hui Cao provides a detailed review of the concepts and advances in the field of random lasers. "Feedback in Random Lasers" (Chapter 12) by Mikhail A.

Noginov emphasizes the significance of the strength of scattering and/or feedback in determining the properties of random lasers. In "Optical Metamaterials with Zero Loss and Plasmonic Nanolasers" (Chapter 13), Andrey Sarychev discusses how nano-horseshoe inclusion in an active host medium results in a plasmonic nanolaser.

Fundamentals. In "Resonance Energy Transfer: Theoretical Foundations and Developing Applications" (Chapter 14), David L. Andrews explores how the intricate interplay between quantum mechanical and electromagnetic medium properties leads to schemes for energy transfer and all-optical switching. In "Optics of Nanostructured Materials from First Principle Theories" (Chapter 15) Vladimir I. Gavrilenko provides a tutorial on the microscopic modelling of optical response functions using density functional theory and related approaches.

Organic photonic materials. Materials whose nonlinear coefficients often exceed their inorganic counterparts both in magnitude and response rate are examined in "Organic Photonic Materials" (Chapter 16) by Larry R. Dalton, Philip A. Sullivan, Denise H. Bale, Scott R. Hammond, Benjamin C. Olbricht, Harrison Rommel, Bruce Eichinger, and Bruce H. Robinson. These authors explore organic optical material design in terms of critical structure/function relationships. "Charge Transport and Optical Effects in Disordered Organic Semiconductors" (Chapter 17) by Harry H. L. Kwok, You-Lin Wu, and Tai-Ping Sun highlights how, as with regular semiconductors, charge transport can be modified by doping in organic materials, which possess enhanced carrier mobilities.

Holographic media. "Holography and Its Applications" (Chapter 18) by H. John Caulfield and Chandra S. Vikram discusses holograms used as parts of complex light-controlled or light-defined systems that manipulate the direction, spectrum, polarization, or speed of pulse propagation of light in a medium.

Slow and fast light. Slow and fast light is an intriguing topic demystified by Joseph E. Vornehm, Jr. and Robert W. Boyd in the final chapter "Slow and Fast Light" (Chapter 19). The authors show how manipulation of the material dispersion can lead to very slow, halted, or even backward propagating optical pulses.

The conception of *Tutorials in Complex Photonic Media* lies in an effort to consolidate the conference series, Complex Mediums: Light and Complexity, a subconference of the annual SPIE Optics and Photonics meeting held over the years 2003–2006<sup>1</sup>. Incentive for this book was also largely compelled by

<sup>&</sup>lt;sup>1</sup> In 2003 the conference was titled Complex Mediums IV: Beyond Linear Isotropic Dielectrics; in 2006 it was titled Complex Photonic Media.

Introduction to Complex Mediums for Optics and Electromagnetics, edited by Werner S. Weiglhofer and Akhlesh Lakhtakia, SPIE Press (2003), which is a consolidation of the Complex Mediums conferences from 1999 to 2002. We have taken special emphasis in this book to avoid the somewhat disjointed presentation that often accompanies books based on conferences. To this end, all of the chapters underwent round-robin reviews by several editors and coauthors who were frequently not directly involved in the research area. Much "back and forth" has hopefully ironed out the specialist's tendency to dive headlong into details that can only be appreciated once sufficient underpinning motivational material has been presented. Another issue is notation. Eventually, we decided that keeping a consistent notation throughout the book would be self-defeating, as anyone entering a new area must, to a certain extent, be flexible to individual authors' preferences. Nevertheless, we went to some lengths to ensure that the notation within each chapter is consistent.

The four editors who undertook this project have had a unique opportunity to work with some of the leading specialists in the field. Of course, there have been frustrations, but in the end, we hope that that this book presents a broad and balanced summary that will lead many others to take up the exciting challenges of working in complex photonic media. In the introduction to the predecessor volume noted above, Akhlesh Lakhtakia wrote 'I shall be delighted if a companion volume were published after another two or three editions of this conference.' Well, here it is.

Mikhail A. Noginov Graeme Dewar Martin W. McCall Nikolay I. Zheludev September 2009

# **List of Contributors**

Leonid V. Alekseyev

Princeton University, USA and Purdue University, USA

David L. Andrews

University of East Anglia Norwich, UK

Durga P. Aryal

University of Surrey, UK

Denise H. Bale

University of Washington, USA

Allan D. Boardman

University of Salford, UK

Levi Bourke

University of Otago, New Zealand

Robert W. Boyd

The Institute of Optics, University of Rochester, USA

Hui Cao

Yale University, USA

H. John Caulfield

Fisk University, USA

Stefano Cavalieri

University of Florence, Italy

Larry R. Dalton

University of Washington, USA

Mark R. Dennis

University of Bristol, UK

**Graeme Dewar** 

University of North Dakota, USA

**Bruce Eichinger** 

University of Washington, USA

Vladimir I. Gavrilenko

Norfolk State University, USA

Azriel Z. Genack

Queens College, City University of New York, USA

Scott R. Hammond

University of Washington, USA

**Ortwin Hess** 

University of Surrey, UK

Ian Hodgkinson

University of Otago, New Zealand

**Zubin Jacob** 

Purdue University, USA

Yutaka Kawabe

Chitose Institute of Science and Technology, Japan

**Neil King** 

University of Salford, UK

Harry H. L. Kwok

University of Victoria, Canada

Stefano Lepri

Institute of Complex Systems, CNR, Italy

Martin W. McCall

Imperial College London, UK

Sushil Mujumdar

Tata Institute of Fundamental Research, India

Evgenii Narimanov

Purdue University, USA

Mikhail A. Noginov

Norfolk State University, USA

Kevin O'Holleran

University of Glasgow, UK

Benjamin C. Olbricht

University of Washington, USA

Gian-Luca Oppo

University of Strathclyde, UK

Miles J. Padgett

University of Glasgow, UK

Bruce H. Robinson

University of Washington, USA

**Harrison Rommel** 

University of Washington, USA

Andrey K. Sarychev

Institute of Theoretical and Applied Electrodynamics, Russia

**Gennady Shvets** 

University of Texas at Austin, USA

Philip A. Sullivan

University of Washington, USA

Tai-Ping Sun

National Chi-Nan University, Taiwan

Renato Torre

University of Florence, Italy

Kosmas L. Tsakmakidis

University of Surrey, UK

Yaroslav A. Urzhumov

COMSOL, Inc. USA

Chandra S. Vikram (deceased)

Fisk University, USA

Joseph E. Vornehm, Jr.

The Institute of Optics, University of Rochester, USA

Diederik S. Wiersma

LENS—European Laboratory for Non-Linear Spectroscopy, BEC-INFM, Italy

You-Lin Wu

National Chi-Nan University, Taiwan

Sheng Zhang

Queens College, City University of New York, USA

# **List of Abbreviations**

AFM atomic force microscopy
APC amorphous polycarbonate

APTE addition de photons par transfers d'énergie

ASE amplified spontaneous emission

ATR attenuated total reflection

BCOG binary chromophore organic glass

BEC Bose-Einstein condensate

BER bit-error rate
BZ Brillouin zone

CCD charge-coupled device
CCW coupled-cavity waveguide
CDM correlated disorder model
CGH computer-generated hologram
CGS centimeter-gram-second

CP circularly polarized

CPO coherent population oscillation

CQED cavity QED

CROW coupled-resonator optical waveguide

CT charge transfer

CVD chemical vapor deposition
DBP delay-bandwidth product
DFB distributed feedback

DFT density functional theory DIOPC double-inverse-opal PC

DOS density of states

DPCM double phase-conjugate mirror DSC differential scanning calorimetry

ECP effective core potential EE electrostatic eigenvalue EET electronic energy transfer

EFISH electric-field-induced second harmonic electromagnetically induced transparency

EM electromagnetic EO electro-optic fcc face-center cubic

FEFD finite element frequency domain

FRET fluorescence RET

FWHM full width at half maximum

FWM four-wave mixing

GDM Gaussian disorder model

GEDE generalized eigenvalue differential equation

GLC geometric LC

GMR gap-to-midgap ratio GVD group velocity dispersion hcp hexagonal close-packed

HOE holographic optical element HOMO highest occupied molecular orbit

HRS hyper-Raleigh scattering

TR infrared

IVR intramolecular vibrational redistribution

JCM Jaynes-Cummings model
LAP laser-assisted poling
LCP left-circular polarization
LDA local density approximation

LED light-emitting diode

LF local field

LHM left-handed material LO longitudinal optical

LUMO lowest unoccupied molecular orbit

ME magneto-electric MO magneto-optic MOCVD metalorganic CVD

MPR magnetic plasmon resonance MSHG magnetization-induced SHG MTHG magnetization-induced THG

NA numerical aperture NIM negative index material

NLO nonlinear optical

NPV negative phase velocity
OCRET optically controlled RET

OCT optical coherence tomography
OEO optical-electrical-optical

OEO optical-electrical-optical organic light-emitting diode optical path length distance optical parameter oscillator

PC (PhC) photonic crystal

PEC perfect electric conductor PFT power Fourier transform

PGB photonic band gap
PMT photomultiplier tubes
PWE plane wave expansion

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QED quantum electrodynamics

QD quantum dot QP quasi-particle QW quantum well

RCP right-circular polarization RET resonance energy transfer

RF radiofrequency
RIE reaction ion etching
rms root mean square

RPA random-phase approximation SBS stimulated Brillouin scattering

SE stimulated emission

SEIRA surface-enhanced IR absorption SEM scanning electron microscope SFG sum frequency generation

SERS surface-enhanced Raman scattering

SHG second-harmonic generation SLM spatial light modulator

SOA semiconductor optical amplifier

SP surface plasmon

SPD square of the polarizability derivative

SPOF strip pair-one film SPP spiral phase plate

SPR surface plasmon resonance

SR slit ring

SRS stimulated Raman scattering

SRR split-ring resonator
TD-DFT time-dependent DFT
TE transverse electric

TF Thomas-Fermi

THG third-harmonic generation TLS two-level amplifying system

TM transverse magnetic

UV ultraviolet

VCSEL vertical-cavity surface-emitting laser

WDM wavelength division multipling

XC exchange and correlation